

A Bayesian methodology for hybrid degradation prognostics

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Clogging of steam generators (SGs)

- ▶ Clogging of SGs is a complex multiphysics phenomenon that occurs following long operational periods in pressurized-water reactors (PWR) of the French nuclear fleet → undermines performance & weakens the structures → *may require chemical cleanings*

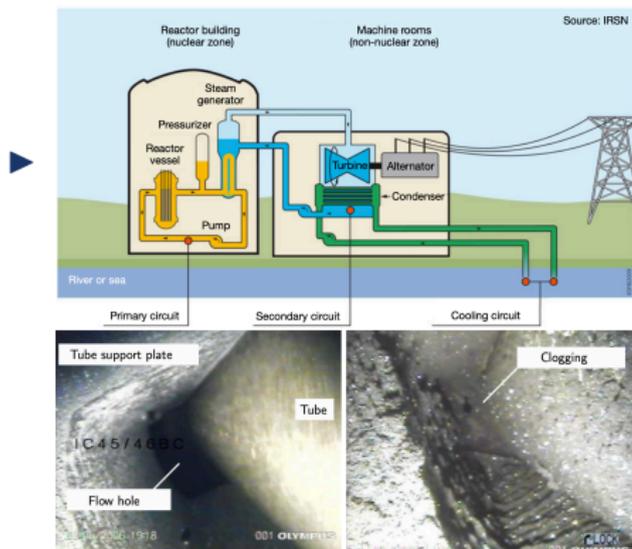


Figure: PWR scheme, and example of video examination during a PWR outage (© IRSN, EDF)

Clogging of SGs

- ▶ No state-of-the-art model allowing for ground insights on diagnostics and prognostics of clogging rate $\tau_c \rightarrow$ very hard to model & challenging to create reproducible lab experiment for model validation + not a lot of literature [Srikantiah and Chappidi, 2000; Prusek et al., 2013; Girard, 2014; Yang et al., 2017]
- ▶ Available scarce video field data as well as indirect measurements \rightarrow allow to construct data-driven regression algorithms [Pincioli et al., 2021] \approx not enough data to have robust predictive models
- ▶ Another tool is the physical clogging model developed by [Prusek et al., 2013] \rightarrow subsequent numerical model THYC-Puffer-DEPO [Feng et al., 2023] \approx lack of enough trustworthy field data for precise V&V
- ▶ Necessary decision-making on chemical cleaning planning under uncertainty \rightarrow ***how to make use of the available knowledge and models for achieving reliable predictions?***

DTs for NPP components

- ▶ Growing interest of creating digital twins (DTs) for the nuclear industry → still many industrial challenges to address

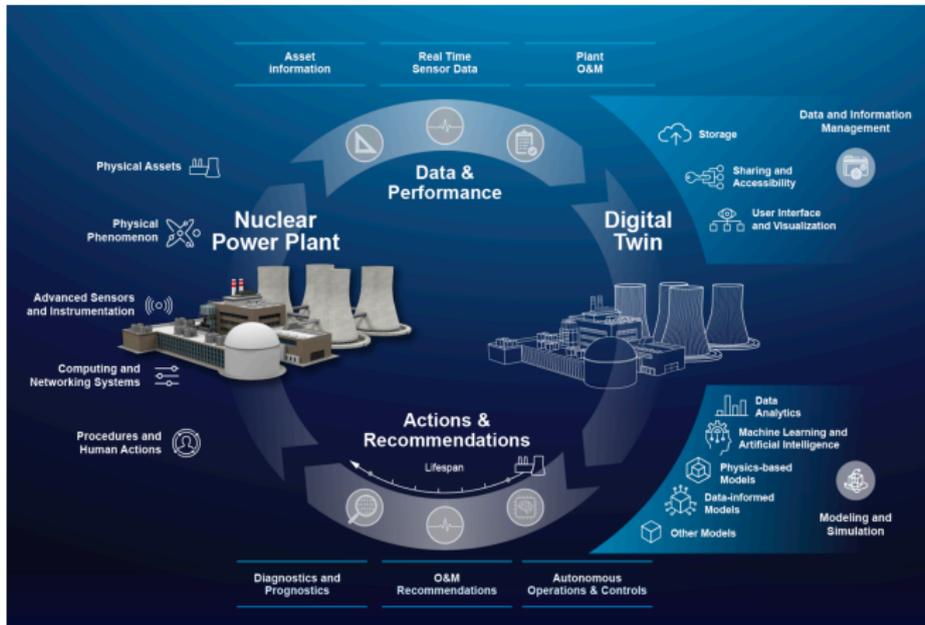


Figure: DT methodologies for nuclear reactors [Vaibhav and al., 2023]

DTs for NPP components

Excerpts from the report [Vaibhav and al., 2023]:

- ▶ *For producing a DT, especially one for an NPP, two broad technological needs must be met are: (1) **modeling and simulation** and (2) **data and information management**.*
- ▶ *The objective of implementing a DT system is to provide actions and recommendations in support of safe, reliable, and efficient system operations. To this end, DT actions and recommendations have been classified into the following categories: **diagnostics** and **prognostics**, operations & management recommendations, and autonomous operations and **controls***
- ▶ ***Diagnostics** and **prognostics** [...] can be enabled in real time by DTs, thus providing plant staff with real time notification and recommendations on emergent or future conditions. Predictive algorithms in DTs can even go beyond diagnostics and prognostics to generate recommendations for efficient O&M practices*

Notions of prognostics

- ▶ Degradation level of the system ($t \mapsto \Delta(t)$) \rightarrow predict the remaining useful life (RUL) [Biggio and Kastanis, 2020] for a fixed threshold $\Delta_* \in \mathbb{R}_+$:

$$\text{RUL}(\Delta) = \underset{t_1 < t \leq t_N}{\operatorname{argmin}} \{ \Delta(t) \geq \Delta_* \} \quad (1)$$

- ▶ Relies on physics-based simulation codes, and/or data driven methods \rightarrow typical DT methodologies
- ▶ RUL prediction with each individual approach could lack robustness \rightarrow high level of uncertainty & individual predictions not fully reliable

Our available tools

- ▶ *Physics-based computer simulation model* $g : \mathcal{X} \subset \mathbb{R}^d \rightarrow \mathbb{R}^N$ with prior uncertainty on input variables $\mathbf{X} = (X_1, \dots, X_d) \sim \mu_{\mathbf{X}}$, one input \mathbf{x}_0 gives a full trajectory:

$$g(\mathbf{x}_0) = (g(t_1, \mathbf{x}_0), \dots, g(t_N, \mathbf{x}_0)) \quad (2)$$

and $\text{pr}_\ell \circ g(\mathbf{X}) := g(t_\ell, \mathbf{X})$ models $\Delta(t_\ell) \rightarrow$ grey-box, physics known but code cannot be modified

- ▶ *q heterogeneous degradation data groups* (from different sensors, statistical models,...) $\mathcal{D} = (\mathbf{y}^1, \dots, \mathbf{y}^q)$ with different sizes $\mathbf{y}^j \in \mathbb{R}^{m_j} \rightarrow$ corresponding to different time indices in \mathcal{J}_i so that $\mathcal{J} = \cup_{i=1}^q \mathcal{J}_i$ and $|\mathcal{J}| = m_1 + \dots + m_q$, such that:

$$\mathbf{y}^j(t_\ell) = \Delta(t_\ell) + \eta_\ell^j, \quad (3)$$

with $\eta_\ell^i \sim \mathcal{N}(0, R^i) \rightarrow$ homoskedastic noise for each data group

- ▶ **How to fuse these tools for hybrid RUL estimation of the system?**

Offline data assimilation

- ▶ Perform offline sequential data assimilation over time windows [Geir Evensen, 2022] using ensemble methods
- ▶ Let $\mathbf{Z} = (\mathbf{X}, \mathbf{Y})$ where $\mathbf{Y} = g(\mathbf{X})$ are the computer model outputs on a prescribed time window, \mathbf{X} are the uncertain parameters that do not vary over time
- ▶ Denote the groups as \mathcal{D} , the goal of data assimilation is to estimate the posterior distribution $p(\mathbf{Z} | \mathcal{D})$
- ▶ Idea; *modular* approach on each time window:
 1. perform Bayesian model updating (BMU) to obtain a posterior distribution $(\mathbf{X} | \mathcal{D}) \sim h_{\mathbf{X}|\mathcal{D}}$,
 2. perform smoothing to obtain the density $p(\mathbf{Y} | \mathbf{X} \sim h_{\mathbf{X}|\mathcal{D}}, \mathcal{D})$, so that the resulting assimilated posterior is approximated as:

$$p(\mathbf{Z} | \mathcal{D}) \simeq h_{\mathbf{X}|\mathcal{D}}(\mathbf{X})p(\mathbf{Y} | \mathbf{X} \sim h_{\mathbf{X}|\mathcal{D}}, \mathcal{D}) \quad (4)$$

Illustration of our methodology

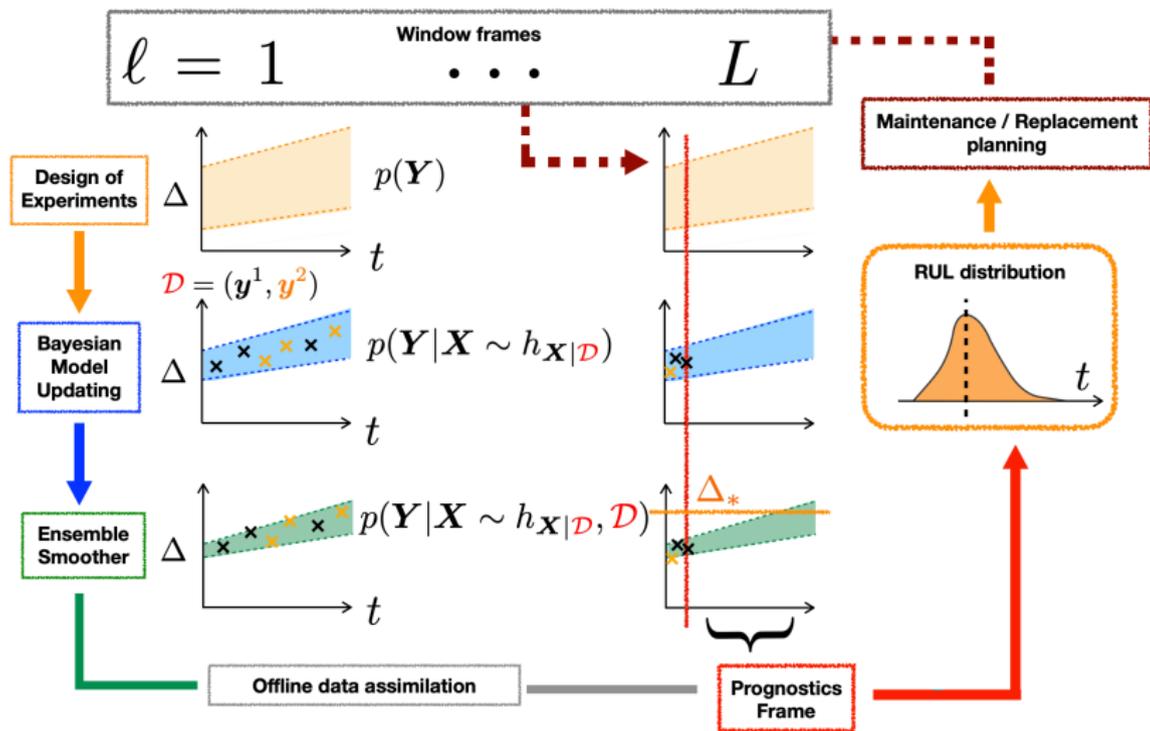


Figure: A sketch of the offline data assimilation methodology.

On the prognostics window

- ▶ Assimilation is performed offline until the prognostics window is reached $\ell = L$, then the RUL distribution can be computed:

$$\mathbb{P}(\text{RUL}(\Delta_*) \leq t_j | \mathcal{D}) = \int_{\mathbb{R}} \mathbf{1}\{\text{pr}_{j+1}(\mathbf{y}) \geq \Delta_*\} p_{\mathbf{y}|\mathbf{x} \sim h_{\mathbf{x}|\mathcal{D}, \mathcal{D}}}(\mathbf{y}) d\mathbf{y} \quad (5)$$

- ▶ Where in practice this probability is estimated using a Monte Carlo ensemble $\{(\mathbf{X}^{(i)}, g(\mathbf{X}^{(i)}))\}_{i=1}^n \sim h_{\mathbf{x}|\mathcal{D}} \otimes g \# h_{\mathbf{x}|\mathcal{D}}$:

$$\mathbb{P}(\text{RUL}(\Delta_*) \leq t_j | \mathcal{D}) \approx \frac{1}{n} \sum_{i=1}^n \mathbf{1}\{\text{pr}_{j+1} \circ g(\mathbf{X}^{(i)}) \geq \Delta_*\} \quad (6)$$

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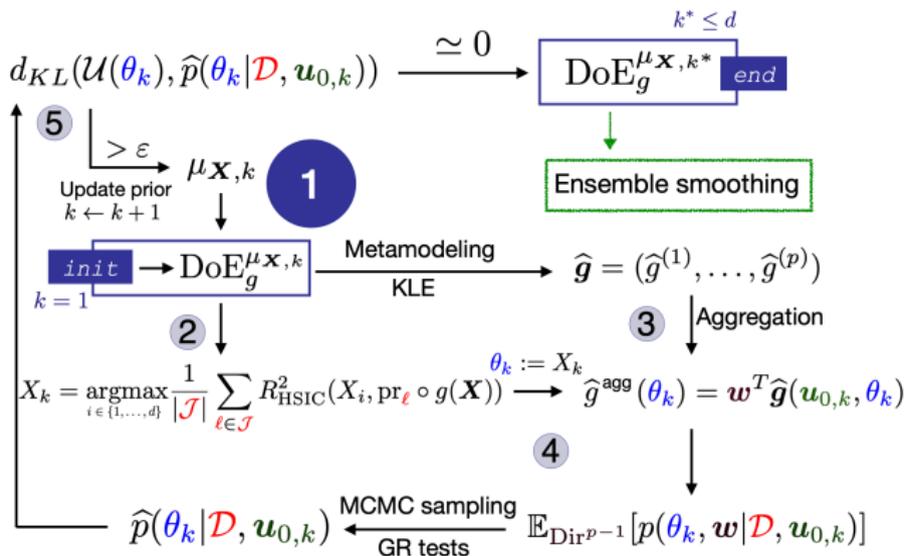
3. Ensemble Kalman smoothing

4. Application to clogging of SGs in NPWRs

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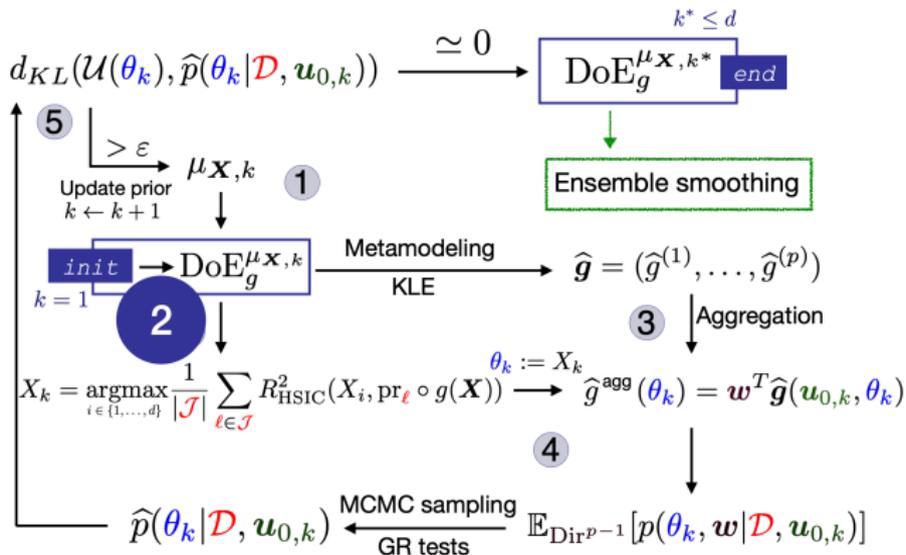
Step 1



Perform k iterations where $1 \leq k \leq d$:

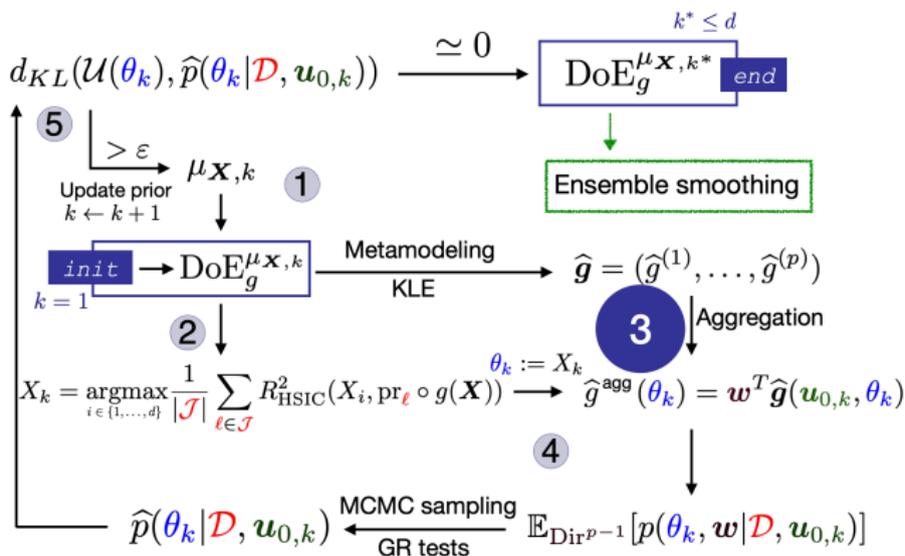
1. If $k = 0$, assume uniform independent priors $\mu_{\mathbf{X},k} \simeq \mathcal{U}[-1, 1]^{\otimes d} \rightarrow$ generate a design of experiments $\text{DoE}_g^{\mu_{\mathbf{X},k}} = \{(\mathbf{X}^{(j)}, g(\mathbf{X}^{(j)}))\}_{1 \leq j \leq n}$

Step 2



2. Compute **HSIC indices** [Gretton et al., 2005] between input variables and outputs at data time instances \rightarrow **given data** sensitivity analysis method to assess *individual* input variable influence on the output

Step 3



3. If g is time-costly, build and validate p metamodels $\hat{\mathbf{g}} = (\hat{\mathbf{g}}^{(1)}, \dots, \hat{\mathbf{g}}^{(p)})$ with chosen strategy \rightarrow avoid metamodeling bias with *convex aggregation* on the unit-simplex choosing $\mathbf{w} \in \Delta^{p-1} := \{\mathbf{w} \in [0, 1]^p, \|\mathbf{w}\|_1 = 1\}$, fix nominal value of $\mathbf{U}_{0,k} = \mathbf{u}_{0,k}$ by taking the mean

Metamodeling step ③

The metamodeling process involves:

- ▶ *Data generation*: Using the DoE of g at n input samples $\{\mathbf{X}^{(j)}\}_{j=1}^n \sim \mu_{\mathbf{X}}$, assemble the data matrix:

$$\mathbf{Y} = \left[g(\mathbf{X}^{(1)}), \dots, g(\mathbf{X}^{(n)}) \right] \in \mathbb{R}^{N \times n} \quad (7)$$

- ▶ *Dimensionality reduction*: Apply a Karhunen–Loève (KL) decomposition [Sullivan, 2015] using the empirical covariance matrix $\hat{\mathbf{C}} = \frac{1}{n} \mathbf{Y} \mathbf{Y}^{\top}$. Perform singular value decomposition (SVD):

$$\mathbf{Y} = \mathbf{V} \mathbf{\Sigma} \mathbf{W}^{\top}, \quad (8)$$

where \mathbf{V} contains the KL modes $\{\Phi_k\}_{k=1}^m$, and $\mathbf{\Sigma}$ holds the singular values.

- ▶ *Mode selection*: Retain m modes to capture a prescribed variance (e.g., 99%). Project trajectories onto the retained modes:

$$\xi_k(\mathbf{X}^{(j)}) = g(\mathbf{X}^{(j)})^{\top} \Phi_k, \quad k = 1, \dots, m \quad (9)$$

Metamodeling step ③

- ▶ *Surrogate modeling*: For each mode k , construct a surrogate model $\hat{\xi}_k(\mathbf{X})$ using a Gaussian process [Rasmussen and Williams, 2006] with identical prior mean and kernel for all modes
- ▶ *Reconstruction*: Reconstruct the full trajectory using the surrogate models:

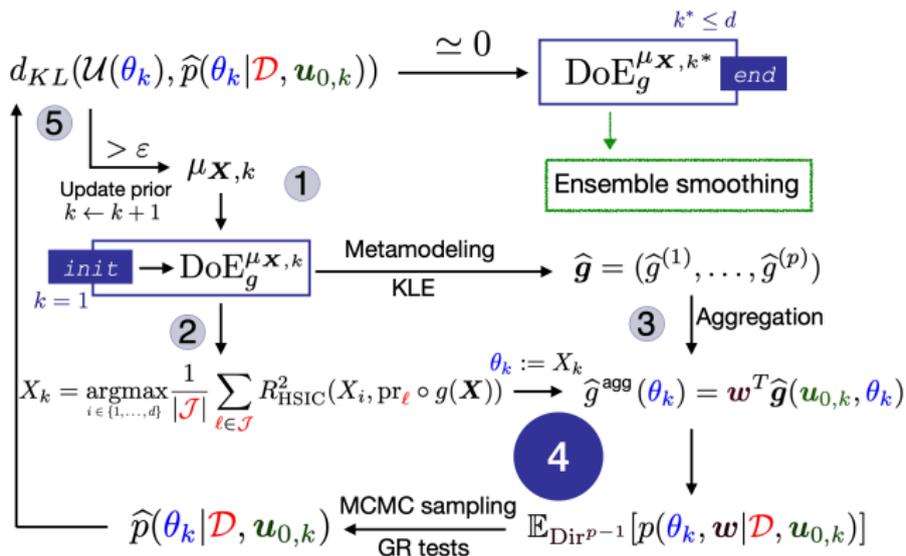
$$\hat{g}(\mathbf{X}) = \sum_{k=1}^m \hat{\xi}_k(\mathbf{X}) \Phi_k \quad (10)$$

- ▶ *Aggregation*: Combine multiple surrogate models $\{\hat{g}^{(i)}\}_{i=1}^p$ using convex aggregation weights $\mathbf{w} \in \Delta^{p-1}$ to form the aggregated surrogate model:

$$\hat{g}^{\text{agg}}(\mathbf{X}) = \sum_{i=1}^p w_i \hat{g}^{(i)}(\mathbf{X}) \quad (11)$$

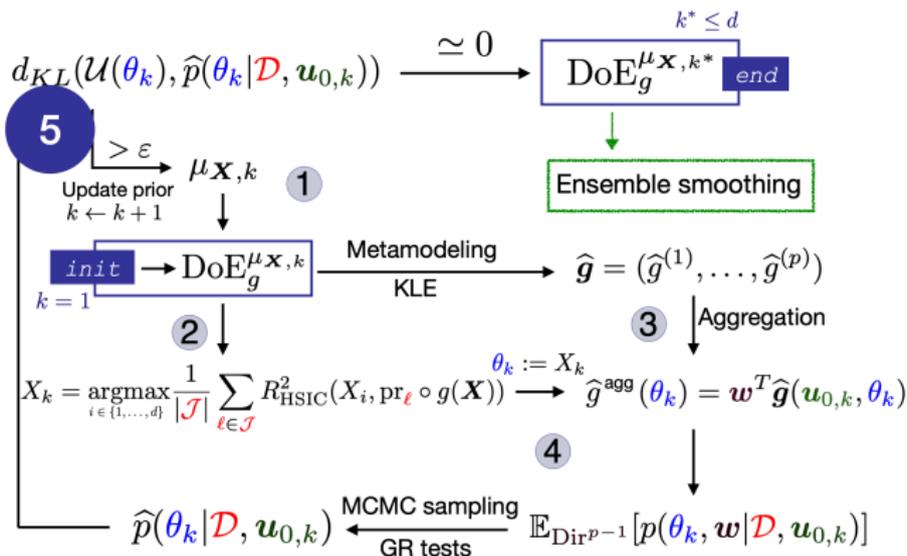
This ensures robustness by leveraging multiple models while minimizing bias

Step 4



- Estimate the posterior distribution $\hat{p}(\theta_k | \mathbf{y}^1, \dots, \mathbf{y}^q, \mathbf{u}_{0,k})$ with an MCMC sampling procedure

Step 5



5. Compute the Kullback-Leibler divergence d_{KL} between prior distribution $\mathcal{U}(\theta_k)$ and the estimated density:

- ▶ If $d_{KL} > \epsilon$, update the prior $\mu_{\mathbf{X},k}$ by replacing marginal $\mathcal{U}(\theta_k)$ with $\hat{p}(\theta_k | \mathbf{y}^1, \dots, \mathbf{y}^q, \mathbf{u}_{0,k})$ and continue $k \leftarrow k + 1$
- ▶ Otherwise, stop and obtain an *updated* RUL prediction by computing $g \# \mu_{\mathbf{X},k^*}$

Proposition

Assume $\lambda := 1/\sigma_\eta^2 \sim \mathcal{G}(\frac{m}{2}, \frac{1}{2}\|\mathbf{y} - \mathbf{f}(\theta)\|^2)$ (Gamma distribution), where m is the number of data points in \mathbf{y} ; $\theta \sim \mathcal{U}(\theta)$, and $p(\theta, \lambda) \propto \lambda^{-1}$.

Then:

$$p(\theta|\mathbf{y}) \propto \|\mathbf{y} - \mathbf{f}(\theta)\|^{-m} \quad (12)$$

Moreover, if multiple groups of data at different time-instances are considered, $\mathbf{y}^1, \dots, \mathbf{y}^q$, with respective priors on the inverse of their standard deviations $\lambda_i \sim \mathcal{G}(\frac{m_i}{2}, \frac{1}{2}\|\mathbf{y}^i - \mathbf{f}(\theta)\|^2)$, then the generalization is:

$$p(\theta|\mathbf{y}^1, \dots, \mathbf{y}^q) \propto \prod_{i=1}^q \|\mathbf{y}^i - \mathbf{f}(\theta)\|^{-m_i} \quad (13)$$

Proof. Bayes' theorem and simplifications.

Bayesian updating step 4

$$p(\theta_k | \mathbf{y}^1, \dots, \mathbf{y}^q, \mathbf{u}_{0,k}) \propto \frac{1}{M} \sum_{r=1}^M \prod_{i=1}^q \|\mathbf{y}^i - \langle \mathbf{w}^{(r)}, \hat{\mathbf{g}}(\mathbf{u}_{0,k}, \theta_k) \rangle\|^{-m_i} \quad (14)$$

- ▶ Use Random Walk Metropolis-Hastings (RWMH) MCMC algorithm [Sullivan, 2015] to sample from (14)
- ▶ Monte-Carlo integration using sample $\{\mathbf{w}^{(r)}\}_{r=1}^M$ from the Dirichlet- $\mathbf{1}_p$ distribution on the simplex \rightarrow integrate hyperparameter
- ▶ Test convergence of RWMH chains with Gelman-Rubin test [Gelman and Rubin, 1992]
- ▶ Updated densities are conditioned on nominal values $\mathbf{u}_{0,k}$ of *other* $d - 1$ input variables \rightarrow future work on how to integrate uncertainty
- ▶ Use log-sum-exp trick for numerical computation

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Ensemble Kalman smoothing

- ▶ We don't need sequential updating at each time-step $p(g(t_k, \mathbf{X})|\mathcal{D})$ (which is the goal of filtering), but to assimilate the data on the entire window frame
- ▶ Indeed the data is *unavailable* at each time-step, so we need to account of all the information on a window
- ▶ The good paradigm for this is smoothing, i.e getting estimates from the full-posterior distribution $p(g(t_1, \mathbf{X}), \dots, g(t_k, \mathbf{X})|\mathcal{D}) \rightarrow$ Ensemble Kalman smoothing (EnKS) [Evensen and van Leeuwen, 2000]

Ensemble Kalman smoothing

- ▶ Build an ensemble $\{g(\mathbf{X}^{(k)})\}_{k=1}^n \sim g \# h_{\mathbf{x}|\mathcal{D}}$, suppose for each data-group $i = 1, \dots, q$:

$$y^i(t_\ell^i) = g(t_\ell^i, \mathbf{X}) + \eta_i, \quad (15)$$

where the variance R^i of the noise *is known*

- ▶ Define the ensemble mean and anomalies:

$$\bar{g}(t) = \frac{1}{n} \sum_{k=1}^n g(t, \mathbf{X}^{(k)}), \quad A^{(k)}(t) = g(t, \mathbf{X}^{(k)}) - \bar{g}(t) \quad (16)$$

- ▶ The cross-covariance between ensemble states at any time t and the observation times t_ℓ^i are approximated empirically:

$$\hat{C}(t, t_\ell^i) = \frac{1}{n-1} \sum_{k=1}^n A^{(k)}(t) A^{(k)}(t_\ell^i) \quad (17)$$

Ensemble Kalman smoothing

- ▶ We define the Kalman gain for each t in the time-window:

$$K_t = \frac{\widehat{C}(t, t_\ell^i)}{\widehat{C}(t, t_\ell^i) + R^i} \quad (18)$$

- ▶ And defining the innovation term as $d_\ell^{(k)} = y^j(t_\ell^i) - g(t_\ell^i, \mathbf{X}^{(k)})$, we update all the ensembles following:

$$g(\mathbf{X}^{(k)}) \leftarrow g(\mathbf{X}^{(k)}) - K_t \cdot d_\ell^{(k)} \quad (19)$$

- ▶ This process is repeated *sequentially* across all observation times t_ℓ^i , for all data groups $i \in \{1, \dots, q\}$

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Results

- ▶ Computer code THYC-Puffer-DEPO, complex multiphysics [Jaber et al., 2024], chaining of 3 codes → allows to simulate SG clogging on entire lifespan of the asset integrating past chemical cleanings and predicting future τ_c levels
- ▶ Two data groups $q = 2$, corresponding to field data and regression data

Input variable	Distribution
α	$\mathcal{U}(100, 103)$
β	$\mathcal{U}(0.02, 0.025)$
ϵ_e	$\mathcal{U}(0.2, 0.5)$
ϵ_c	$\mathcal{U}(0.01, 0.3)$
d_p	$\mathcal{U}(0.5, 10.0) \times 10^{-6}$
$\Gamma_p(0)$	$\mathcal{U}(1.0, 8.0) \times 10^{-9}$
a_v	$\mathcal{U}(0, 15) \times 10^{-4}$

Table: Probabilistic modeling of uncertain input variables

Results: posterior distributions

- ▶ $L = 3$ time windows, 5 MCMC chains are launched for GR convergence test, use uniform proposal distributions
- ▶ Computing time around 40 min \rightarrow 5/7 distributions are informed by the data, distinct modes for a_v

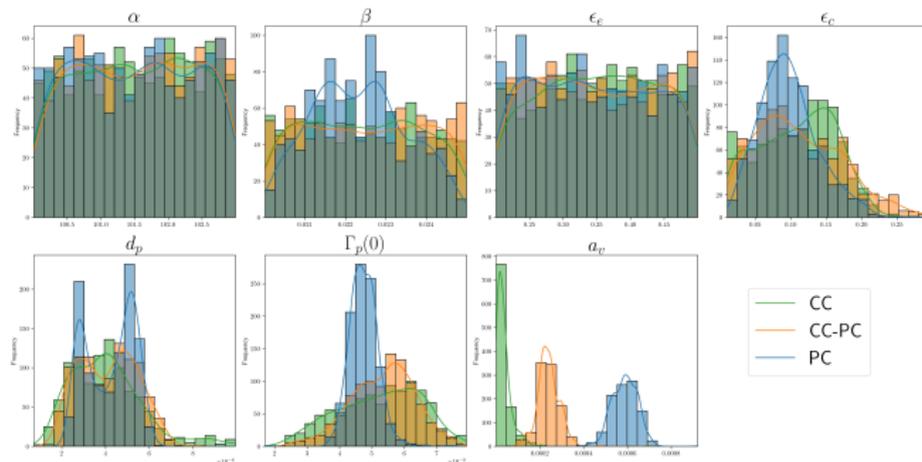


Figure: Posterior distributions of TPD clogging simulation code

Results: posterior trajectories

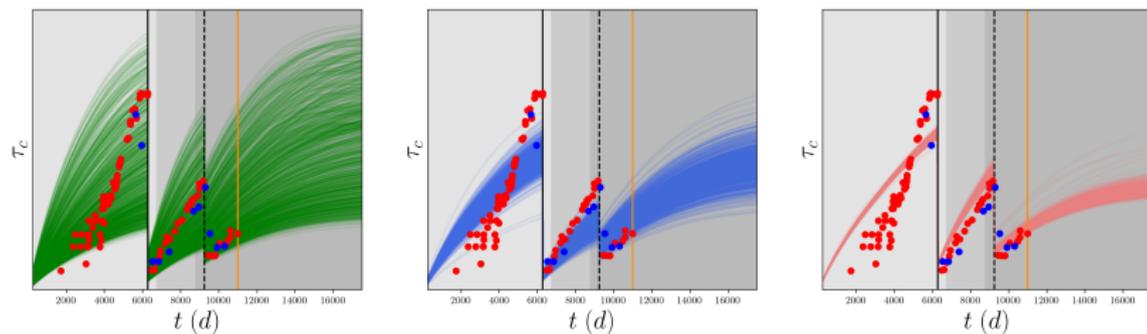
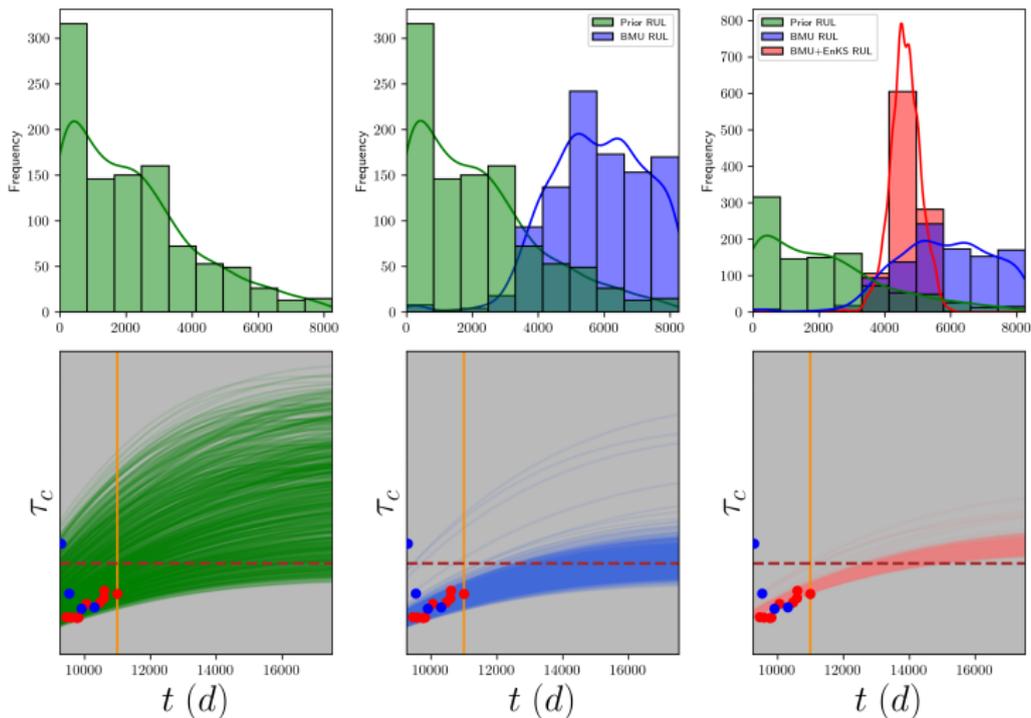


Figure: Prior/posterior and smoothed TPD emulations with Karhunen-Loève expansion surrogate

Results: posterior RUL



- RUL prediction uncertainty substantially reduced and mean of the distribution is shifted compared to the prior → positive impact for maintenance planning

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Summary

- ▶ Developed a modular offline data assimilation procedure combining an iterative BMU algorithm with an ensemble smoothing step for robust system RUL prediction
- ▶ The BMU method acts sequentially on each marginal to keep independence assumption for all dimensions → avoids cross-correlation in MCMC and curse of dimensionality
- ▶ Methodology works with a metamodeling step, enriched at each iteration by an optimization + aggregation of the metamodels on the refined DoEs to avoid bias in the posteriors
- ▶ The method integrates the noise uncertainty and works with heteroskedastic groups of data points
- ▶ Demonstrated the approach on industrial steam generator clogging, showing improved posterior inference and reduced RUL uncertainty
- ▶ Methodology is general and can be adapted to other industrial prognostics problems with scarce and heterogeneous data → [GitHub repository](#)

Perspectives: the SG digital twin

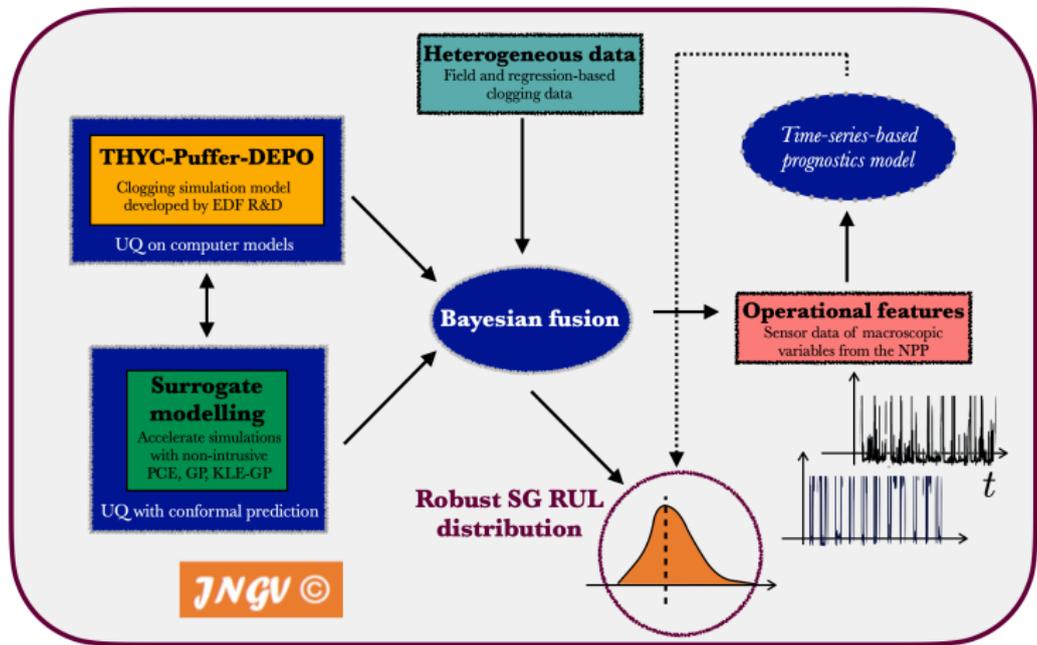


Figure: *Fit for purpose* SG DT for clogging prognostics and health management [Deri et al., 2021].

Thank you for your attention!
Any questions?



Figure: Preprint



Figure: GitHub

reach me out at edgar.jaber@ens-paris-saclay.fr

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Sensitivity analysis: HSIC

- ▶ Hilbert-Schmidt Independence Criterion (HSIC) [Gretton et al., 2005], kernel method → evaluates sensitivity of a single-input in a given-data context, no need for surrogate models
- ▶ Theoretical result for all $i \in \{1, \dots, d\}, k \in \{1, \dots, N\}$:

$$\text{HSIC}(X_i, g(\mathbf{X}, t_k)) = 0 \iff X_i \perp g(\mathbf{X}, t_k) \quad (20)$$

- ▶ The index disposes of U-stat and V-stat estimators + hypothesis testing with corresponding p -value → implemented in the **OpenTURNS**
- ▶ The normalized R_{HSIC}^2 index is better suited for interpretation:

$$R_{\text{HSIC}}^2(X_i, g(\mathbf{X}, t_k)) = \frac{\text{HSIC}(X_i, g(\mathbf{X}, t_k))}{\sqrt{(\text{HSIC}(X_i, X_i)\text{HSIC}(g(\mathbf{X}, t_k), g(\mathbf{X}, t_k)))}} \in [0, 1]$$

- ▶ Empirical evidence suggests that R_{HSIC}^2 can be used confidently for variable ranking → HSIC-ANOVA decompositions also exist *but* only pathological cases create stark differences (see [Sarazin et al., 2022])

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